

Figure 1. Perspective of $3 \beta, 16 \beta, 23(R), 26$-tetrahydroxy- $5 \beta$-cholestane.
involve concomitant formation of a transitory vinyl ether such as 6 that easily cleaves to olefin 7. Addition of in situ generated diborane (hydroboration sequence) to the olefin intermediate (7) would proceed mainly from the least hindered carbon po-

sition (and side) to yield as major product the $23 R$ alcohol. The experimental observations, including the fact that dihydrosmilagenin (3) is not an intermediate in this unusual reaction, seem consistent with such a mechanistic pathway.

Single crystals of the C-23R isomer of tetraol $\mathbf{4 b}$ were obtained from a saturated acetone and methanol solution. Precession photographs revealed Laué symmetry and systematically extinct reflections corresponding uniquely to monoclinic space group $P 2_{1}$ with cell constants $a=17.826$ (5) $\AA, b=$ 7.682 (2) $\AA, c=10.996$ (4) $\AA$, and $\beta=122.38(2)^{\circ}$. Crystal density, measured by flotation in carbon tetrachloride-toluene, was found to be $1.12 \mathrm{~g} \mathrm{~cm}^{-3}$ ( $\rho_{\text {calcd }}=1.14 \mathrm{~g} \mathrm{~cm}^{-3}$, for $Z=2$ ). Diffraction intensity measurements were made on a Syntex $\mathrm{P} \overline{1}$ four-circle diffractometer using graphite monochromated $\mathrm{CuK} \alpha(\lambda=1.54178 \AA)$ radiation. Reflections were scanned in a variable speed (between 1 and 12 deg $\min ^{-1}$ ) $2 \theta-\theta$ mode. Of 2849 reflections measured with $(\sin \theta) / \lambda<0.50$ in one quadrant of reciprocal space, 2645 unique reflections were accepted with $\left|F_{\mathrm{o}}\right|>0$. Corrections were made for Lorentz and polarization effects but not for absorption ( $\mu=5.4 \mathrm{~cm}^{-1}$ ) or extinction.
Direct methods were used to solve the structure using MULTAN-74. ${ }^{8}$ Large-block least-squares refinement ${ }^{9}$ with anisotropic thermal parameters, fixed $\mathrm{C}-\mathrm{H}$ hydrogen positions (placed at idealized locations $1.0 \AA$ from respective C atom), and variable $\mathrm{O}-\mathrm{H}$ hydrogen positions (located by a difference Fourier synthesis) converged at residual $R=0.058$ and $R_{w}=$ 0.048 , where weighted residual $R_{w^{\prime}}=\left(\sum w\left(\left|F_{\mathrm{o}}\right|-\left|F_{\mathrm{c}}\right|\right)^{2} /\right.$ $\left.\Sigma w\left|F_{0}\right|^{2}\right)^{1 / 2}$ and $w=1 / \sigma_{F_{0}}{ }^{2}$. Since $3 \beta, 16 \beta, 23(R), 26$-tetra-hydroxy- $5 \beta$-cholestane was obtained by reduction of the $5 \beta$ cholestane, smilagenin, the absolute configuration and conformation displayed in the perspective view in Figure 1 are those of the correct enantiomer.

Naturally occurring sterols bearing oxygen at C-22 or C-23 such as the insect molting hormone $\alpha$-ecdysone ${ }^{10}(8)$ and the


8.t-Ecaysone
$\stackrel{9}{2}$
new soft coral component $9^{11}$ require extensive structural maneuvers to elaborate the necessary side-chain oxygen sub-
stituents. The unique one-step conversion of steroidal sapogenins to C-22 and C-23 alcohols greatly improves the accessibility of such intermediates for synthetic purposes.

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## Quantitative Assessment of pp- $\sigma$ Overlap in a Topologically Convex Triene. Electronic and Crystal Structure Analysis of $\boldsymbol{C}_{16}$-Hexaquinacene

Sir:
$C_{16}$ - Hexaquinacene (1) is the third and newest member ${ }^{1}$ of a select group of trienes, which includes triquinacene (2) and cis $^{3}$ - 1,4,7-cyclononatriene (3), whose constituent double bonds adopt an arrangement potentially suitable for effective $\mathrm{pp}-\sigma$ overlap. ${ }^{2}$ Thus, the question arises as to whether one or more members of this series might partake of neutral homoaromatic character. ${ }^{3}$ Photoelectron (PE) spectroscopic investigations of $3^{4}$ have revealed a sizable interaction between its $\pi$ bonds. The energy difference between the bands corresponding to ionization from the $\mathrm{e}(\pi)$ and $\mathrm{a}_{1}(\pi)$ orbitals was found to be 0.9 eV . This split corresponds to a resonance integral $(\beta)$ of -0.3 eV , a value consistent with the distance $(2.46 \AA)^{5}$ between the ethylene units. Although the distance in $2(2.533 \AA)^{6}$ is close to that found for 3 , a split of only $0.35-0.4 \mathrm{eV}$ has been found. ${ }^{7}$ This difference between $\mathbf{2}$ and $\mathbf{3}$ has been explained by hyperconjugative effects. ${ }^{7.8}$ Thus, in 3 the interactions of $e(\pi)$ and $a_{1}(\pi)$ with the $\sigma$ frame are of similar magnitude, while in

$\stackrel{1}{\sim}$

$\underset{\sim}{2}$

$\stackrel{3}{2}$


Figure 1. Top: view of $C_{16}$-hexaquinacene down the threefold axis showing the atomic numbering. Important bond distances and angles follow: C . 1 -C-2, $1.544 \AA$; C-2-C-3A. $1.574 \AA$; C-2-C-3B, $1.542 \AA$; C-3A-C-3B" , $1.561 \AA$; C-3A-C-4A, $1.505 \AA$ : C-3B-C-4B, $1.513 \AA$; C- $4 \mathrm{~A}-\mathrm{C}-4 \mathrm{~B}, 1.323$ $\AA ;$ C. $2^{\prime}$-C.1-C-2, $108.0^{\circ}$ : C-1-C-2-C-3A, $107.8^{\circ}$; C-1-C-2-C-3B, 109.2 ${ }^{\circ}$ : C-2-C-3B-C-3A ${ }^{\prime}, 107.6^{\circ}$; C-2-C-3A-C-3B", $107.4^{\circ}$; C-3A-C-2-C-3B, $107.2^{\circ} ;$ C- $2-\mathrm{C}-3 \mathrm{~A}-\mathrm{C}-4 \mathrm{~A}, 102.7^{\circ} ; \mathrm{C}-2-\mathrm{C}-3 \mathrm{~B}-\mathrm{C}-4 \mathrm{~B}, 103.6^{\circ}$ : $\mathrm{C}-3 \mathrm{~A}-\mathrm{C}-4 \mathrm{~A}-\mathrm{C}-4 \mathrm{~B}, 113.5^{\circ}$; C-3B-C-4B-C-4A, $112.8^{\circ}$. Average $\sigma(\mathrm{C}-\mathrm{C})$ $\approx 0.003 \AA$ and $\sigma(\mathrm{C}-\mathrm{C}-\mathrm{C}) \approx 0.2^{\circ}$. Bottom: view of the molecule perpendicular to the threefold axis emphasizing its hemispherical shape. The $\mathrm{C}-4 \mathrm{~A}-\mathrm{C}-4 \mathrm{~B}^{\prime}$ distance is $2.848 \AA$ (see text). Thermal ellipsoids are all (including hydrogen atoms) shown at the $50 \%$ probability level.

2 the interaction of $\mathrm{a}_{1}(\pi)$ with the $\sigma$ frame is stronger than that involving $e(\pi)$.

The X-ray crystal structure data for $\mathbf{2}$ and $\mathbf{3}$ have provided not only the internuclear distance $(R)$ in the gap, but also accurate information on the relative canting of the opposed $p$ orbitals. The extent of interpenetration of these orbitals, as given by the overlap ( $S$ ), has been established through vector analysis to be 0.054 and 0.066 , respectively. ${ }^{2}$ Models indicate that the enhanced sphericality of $\mathbf{1}$ leads to a much improved in-plane alignment of the $\mathrm{p} \pi$ orbital triad. The important question of whether these orbitals are in adequate proximity to engage in homoconjugative stabilization is resolved herein.

That $\mathbf{1}$ does not exist as a highly delocalized ground-state molecule is already apparent in its ${ }^{1} \mathrm{H}$ and ${ }^{13} \mathrm{C}$ NMR spectra. ${ }^{1}$ The four carbon resonances $(131.57,60.15,54.91$, and 53.06 ppm ) and the attendant ${ }^{13} \mathrm{C}-\mathrm{H}$ coupling constants ( 160.1 , $138.2,134.3$, and 137.7 Hz , respectively) appear quite normal. Its vacuum ultraviolet spectrum recorded in cyclohexane solution is characterized by a lone absorption maximum at 192 $\mathrm{nm}(\epsilon 20000)$, the lack of vibrational fine structure comparing favorably with the electronic spectra given by triquinacene $\left(\lambda_{\max }^{\text {isoctane }} 187 \mathrm{~nm}(\epsilon 13000)\right)^{9 \mathrm{a}}$ and cyclopentene $\left(\lambda_{\max } 180 \mathrm{~nm}\right.$ $(\epsilon 10000)) .{ }^{9 b}$


Figure 2. The $\mathrm{He}(\mathrm{I})$ photoelectron spectrum of $C_{16}$-hexaquinacene.

Columnar hexagonal crystals of $\mathbf{1}$, grown from acetone solution, gave the rhombohedral cell constants $a=7.285$ (1) $\AA$ and $\alpha=112.59(1)^{\circ}\left(\lambda(\operatorname{MoK} \bar{\alpha})=0.71069 \AA, T=-107^{\circ} \mathrm{C}\right)$. The density and lack of systematic absences indicated probable space groups $R 3$ and $R 3 \mathrm{~m}$. All accessible reflections with $4.0^{\circ}$ $\leq 2 \theta \leq 75.0^{\circ}$ were measured at least three times and at several different crystal settings about the scattering vector. Averaging of over 7000 low temperature $\left(-107^{\circ} \mathrm{C}\right)$ measurements ${ }^{10}$ gave a final data set of 595 unique reflections. Data reduction and weighting were performed in the standard way. ${ }^{11}$ The structure, solved by inspection of the Patterson function and refined by conventional Fourier and least-squares techniques, ${ }^{12}$ showed $C_{16}$-hexaquinacene to possess very nearly 3 m point symmetry, although the space group is actually $R 3$ (hexagonal indexing: $a=12.122$ (1) and $c=6.073$ (1) $\AA, C_{3}^{4}$, No. 146). The final disagreement indices are $R(F)=0.062, R_{W}\left(F^{2}\right)=0.062$, and $\mathrm{GOF}=1.92$. The final difference Fourier map (average noise level, ca. $\pm 0.1 \mathrm{e}^{-} / \AA^{3}$ ) shows no residual electron density $>0.30$ $\mathrm{e}^{-} / \AA^{3}$, with these peaks nearly all localized in the bonding regions.

Figure 1 depicts the molecular geometry and gives the bond distances and angles. The deviations from idealized 3 m symmetry are most apparent in the bond distances about C-2, which differ by nearly $10 \sigma$. The central cyclopentane rings are planar within experimental error, but the cyclopentene rings are puckered very slightly outward; we observe the planar $\mathrm{C}-3 \mathrm{~A}-\mathrm{C}-4 \mathrm{~A}-\mathrm{C}-4 \mathrm{~B}-\mathrm{C}-3 \mathrm{~B}$ olefin fragment to make a $5.4^{\circ}$ dihedral angle with the plane defined by C-3A-C-2-C-3B. For comparison, the same angle in cyclopentene is $29.0^{\circ},{ }^{13}$ and in triquinacene (2), 2.20.6

The intramolecular C-4B-C-4A' distance is $2.85 \AA$, or $\sim 0.3$ $\AA$ shorter than the usual $3.1-\AA$ aromatic stacking distance. The normals to the three olefin units intersect on the threefold axis at a point $2.23 \AA$ from the midpoints of the double bonds; the angles between these normals and the threefold axis are $107.0^{\circ}$.
On the basis of these findings, the magnitude of the $p-p$ overlap integral between the $\mathrm{C}-4 \mathrm{~B}-\mathrm{C}-4 \mathrm{~A}^{\prime}$ atom pair is seen to be only 0.054 . Although the geometry is more favorable, the longer interatomic distances clearly have an untoward effect.

To gain a more accurate estimate of the prevailing through-space effects, the $\mathrm{He}(\mathrm{I}) \mathrm{PE}$ spectrum of 1 was determined (Figure 2) and found to exhibit a single peak separated by $\sim 1 \mathrm{eV}$ from strongly overlapping bands, in a manner very similar to the pattern given by 2 . Because the $\pi$ units in $\mathbf{1}$ are


Figure 3. Orbital energy plot showing the variations in $e(\pi)$ and $a_{1}(\pi)$ levels as a function of distance between interacting $\pi$ bonds.


Figure 4. Correlation of the ionization energies of 1-3.
Table I. Comparison between the Ionization Potentials and Molecular Orbital Energies of $C_{16}$-Hexaquinacene (1) ${ }^{a}$

| band | $I_{V}$ | assignment | $-\epsilon_{\mathrm{j}}$ (MINDO/3) |
| :---: | :---: | :---: | :---: |
| (1) |  | $\mathrm{a}_{1}(\pi)$ | 8.94 |
| (2) | 8.74 | e( $\pi$ ) | 9.41 |
| (4) | 9.9 | $\mathrm{a}_{2}(\sigma)$ | 9.75 |

${ }^{a}$ All values are in electron volts.
separated by $2.85 \AA$, the split between $e(\pi)$ and $\mathrm{a}_{1}(\pi)$ should be below $0,5 \mathrm{eV}$. The first band is therefore assigned to ionization from $\mathrm{e}(\pi)$ as well as $\mathrm{a}_{1}(\pi)$ (see Table I). This assignment is supported by MO calculations of the MINDO/3 type, ${ }^{14}$ assuming the validity of Koopmans' theorem. ${ }^{15}$

These calculations predict $\mathrm{a}_{1}(\pi)$ to reside above e $(\pi)$ owing to the strong interaction of $a_{1}(\pi)$ with $a_{1}(\sigma)$ as in the case of 2. In Figure 3, we have plotted the orbital energy of $e(\pi)$ and $a_{1}(\pi)$ of 1 as a function of the distance between the $\pi$ segments. For this purpose, extended Hückel calculations were utilized. ${ }^{16}$ Like the MINDO/ 3 method, this procedure predicts a crossing of $\mathrm{a}_{1}(\pi)$ and $\mathrm{e}(\pi)$ at $2.6 \AA$, thereby also implicating the sequence $\mathrm{a}_{1}(\pi), \mathrm{e}(\pi)$ for 1 .

The ionization energies of 1-3 are correlated in Figure 4. As a result of the more extended $\sigma$ framework in 1 relative to 2 and 3 , the center of gravity is shifted toward lower energy. As a direct consequence of the larger distance between its $\pi$ bonds, homoconjugation in $\mathbf{1}$ is completely overridden by hyperconjugation.

The essentially ineffective $\sigma$ overlap of the $\mathrm{p} \pi$ orbitals in 1 has decided chemical ramifications. Thus, the triene is totally inert to attempted reduction with potassium in liquid ammonia or oxidation with $\mathrm{Co}(\mathrm{Az})_{3}$ in a flow-through system. ${ }^{17}$

The electronic nature of $\mathbf{1}$ would appear to rule out the likelihood that neutral homoaromatic character will ever be uncovered.

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(10) internai agreement indices for the multiply measured data are

$$
\begin{gathered}
R^{\prime}=\left[\left(\sum_{n k k} \sum_{j=1}^{n}\left|F_{1}-F_{a v}\right| /\left(\sum_{n k 1}\left(n_{1}-1\right) F_{a v}\right)\right]=0.048\right. \\
R^{\prime \prime}=\left[\left(\sum_{n k 1}^{n} \sum_{j=1}^{1} w\left|F_{i}^{2}-F_{a v}^{2}\right|^{2}\right) /\left(\sum_{n k 1} w\left(n_{j}-1\right) F_{a v}^{4}\right)\right]=0.049
\end{gathered}
$$

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## Static and Dynamic Stereochemistry of Dicoordinate Phosphorus Cations

Sir:
It has been demonstrated ${ }^{1,2}$ that halide ion abstraction from halophosphines results in apparently dicoordinate phosphorus

